

Prof. Kincaid - January 25

## 2.5 - Variation

- $y$  varies directly as  $x \Rightarrow y = kx$  Constant  
↓  
V
- $y$  varies inversely as  $x \Rightarrow y = \frac{k}{x}$
- $y$  varies jointly as  ~~$x$  and  $z$~~   $\Rightarrow y = k \cdot xz$

\* Making a model, and then using it to project or predict things.

### The Procedure

- ① Set up the equation with constant  $k$
- ② Use appropriate data to find  $k$  (initial conditions)
- ③ rewrite the equation, replacing  $k$  with its new value.
- ④ Find the requested information. { Try making your own procedure so as not to miss any steps! }

④ 'V' varies directly with 't'.  $V=16$  when  $t=2$ .

$$\rightarrow y = kx \Rightarrow V = kt \quad \left\{ \begin{array}{l} \text{we need to find } k, \text{ so what} \\ \text{do we need? In this case,} \\ \text{V and } t, \text{ so I can solve} \\ \text{for the last missing thing!} \end{array} \right.$$

$$\rightarrow 16 = k(2) \Rightarrow \boxed{8 = k}$$

$$\rightarrow \boxed{V = 8t}$$

→ #6

8)  $y$  varies inversely with  $\sqrt{x}$ .  $y = 4$  when  $x = 9$ .

$$\rightarrow y = \frac{k}{x} \rightarrow y = \frac{k}{\sqrt{x}}$$

$$\rightarrow 4 = \frac{k}{\sqrt{9}} \rightarrow 4 = \frac{k}{3} \Rightarrow \boxed{12 = k}$$

$$\rightarrow \text{Rewrite} \Rightarrow y = \frac{12}{\sqrt{x}}$$

10)  $T$  varies jointly as  $\sqrt[3]{x}$  and  $d^2$ .  
 $T = 18$  when  $x = 8$  and  $d = 3$ .

$$\rightarrow y = k \cdot x^a \rightarrow T = k \cdot \sqrt[3]{x} \cdot d^2$$

$$\rightarrow 18 = k \cdot \sqrt[3]{8} \cdot (3)^2$$

$$18 = k \cdot 2 \cdot 9 \Rightarrow 18 = k \cdot 18 \Rightarrow \boxed{k = 1}$$

$$\rightarrow T = \sqrt[3]{x} \cdot d^2$$

~~.....~~

32) P. 193 in Sullivan text book. ....

Information: current =  $i$  amperes  
resistance =  $Z$  ohms

$$y = \frac{k}{x}$$

• Current is inversely proportional to resistance

$$\rightarrow i = \frac{k}{Z}; \quad i = 30, \quad Z = 8$$

$$30 = \frac{k}{8} \Rightarrow 240 = k$$

$$\rightarrow \boxed{i = \frac{240}{Z}} \Rightarrow \text{if } Z = 10, \text{ then } \dots$$

$$\rightarrow i = \frac{240}{10} = 24 \text{ amperes}$$